

Original Research Article: Using the Coupled-Channelled Optical Model Code to Investigate the Nuclear Property of Protactinium-233 for Reactor Fuel Application

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ABSTRACT

This work uses the coupled-channelled optical model code to investigate the nuclear property of protactinium-233 for reactor fuel application. The high demand for nuclear reactor fuels has necessitated this research. As one of the major naturally occurring radionuclides with lots of fuel prospect, Protactinium-233 with half-life of 26.975 days occur in trace. By neutron induction, protactinium-233 can produce fissile materials to be used as reactor fuel. Computations were done for both the Potential Expanded by Derivatives (PED) which account for the Rigid-Rotor Model (RRM) that treat nuclei as rigid vibrating sphere and account for nuclear volume conservation and Rotational Model Potentials (RMP) which account for the Soft-Rotator Model (SRM) that treat nuclei as soft rotating spherical deformed shapes. Each of the calculated data was compared with the retrieved data from Evaluated Nuclear Data File (ENDF) which was found to be in good agreement. The threshold energies in all cases were found to be ≤ 4 MeV for both PED (Potential Expanded by Derivatives) and RMP (Rotational Model Potentials). It is observed that results from RMP much better agreed with the retrieved data than one obtained from PED.

Introduction

The needs for Fissile isotopes of uranium are due to their practical applications. These isotopes or materials can be used as fuel in

nuclear reactors of both power plants and research reactors, as they can be split by neutrons in a self-sustaining nuclear chain reaction. The amount of energy released during these reactions is large enough to generate

electricity. Aside from being used as nuclear reactor fuels, fissile materials can undergo fission reaction processes. They are the key components of nuclear weapons or other nuclear explosives devices. Those mostly used in nuclear weapons are highly enriched uranium (uranium-235 and plutonium-239). However, this research is for nuclear research reactor application. As such, we shall focus on nuclear reactor fuels [1]. It is pertinent to search for alternative fuel means in some isotopes that are radioactive aside the uranium-235 and plutonium-239. We may recall that the two most important fissile materials normally used as fuels are uranium-235 and Plutonium-239. These are weapon-grade materials that can be also used as reactor fuels. Uranium 235 is a natural isotope of uranium with an abundance of 0.72%. This concentration is very small. Nuclear physicists have made efforts to increase this concentration through the enrichment process. However, due to the prevalent need for reactor fuels, we ought to seek alternative isotopes that can be used as fuels [2].

The fissile materials Plutonium-239 and uranium-233, which do not occur in nature, are produced by the transmutation of uranium-238 and thorium-232, respectively. These materials are called fertile materials. For fuel cycles using plutonium-239 and uranium-233 as fuel, irradiation of uranium-238 and thorium-232 in the fuel blanket and reprocessing to extract the plutonium-239 and uranium-233 become important steps in the cycle [3]. Plutonium-239 is not a natural isotope of plutonium. It is bred from the naturally occurring uranium-238 whose natural abundance is 99.9%. Uranium-238 is irradiated by fast neutrons to produce Uranium-239 and this Uranium-239 can undergo a radioactive decay to produce Plutonium-239. Plutonium-239 just like Uranium-235 is a fissile material. The Plutonium-239 can then be bombarded with high-speed neutrons. When a Plutonium nucleus absorbs one such free neutron, it splits into two fission fragments. This fission releases heat as well as neutrons, which in turn splits other plutonium nuclei present, freeing still more neutrons. As this process is repeated, it

becomes a self-sustaining chain reaction, yielding a steady source of energy, chiefly in the form of heat which is transported from the reactor core by a liquid sodium coolant to a system of heat exchange. This system utilizes heat to produce steam for a turbine that drives an electric generator [4-5].

Uranium-233 is a fissile isotope of uranium bred from thorium-232 as part of the thorium fuel cycle. Uranium-233 was investigated for use in nuclear weapons and as reactor fuel. It has been successfully used or tested in experimental nuclear reactors and has been proposed for much more or wider use as nuclear fuel. It has a half-life of 160,000 years [3]. Uranium-233 is produced by neutron irradiation of thorium-232. When thorium-232 absorbs a fast neutron, it becomes thorium-233 with a half-life of 22 minutes. After 22 minutes, thorium-233 decay by alpha to protactinium 231 with a half-life of 27 days, and beta decays to uranium 233. Just like uranium-235 and plutonium 239, protactinium-233 has also been proposed to be used as nuclear fuel as asserted above [6]. Therefore, protactinium-233 being naturally occurring isotope, is a breeder fissile material [7].

A research was conducted by Avrigeanu and Avrigeanu (2019) [8] on the analysis of neutron bound states of ^{208}Pb by a dispersive optical model potential, in their research, they discussed the effect of dispersive-correction terms on the calculation of bound-state energies and finally reported that the derived ^{208}Pb root mean square radius shows good agreement with measured data. Another research was carried out by Avrigeanu and Avrigeanu *et al.* (2021) [9] on the dispersive optical model description of nucleon scattering on Pb-Bi isotopes and reported that the new potential is shown to give a very good description of nucleon scattering data on near-magic targets $^{206,207}\text{Pb}$ and ^{209}Bi .

This work uses the coupled-channelled optical model code to investigate the nuclear property of protactinium-233 for reactor fuel application with adjustment for soft and rigid rotation of the nucleus.

Theory

The current optical potential encompasses corrections (relativistic) as reported by Avrigeanu and Avrigeanu (2022) [10] and expanded by Avrigeanu and Avrigeanu *et al.* (2018) [11].

Surface variation $W_D(E)$ and potential for volume absorption $W_V(E)$ can wisely be presented in terms of energy which could be suitable for the dispersive optical model analysis [12,13]. The most utilized energy (dependence) for the surface (imaginary) term has been pointed out by Avrigeanu and Avrigeanu *et al.* (2023) [14] as follow:

$$W_D(E) = A_D \left[\frac{(E-E_f)^{-2}}{(E-E_f)^{-2} + (B_D)^2} - \exp(-\lambda_D(E - E_f)) \right] \quad (1)$$

Where, A_D , B_D , and λ_D are constants (undetermined), and also E and E_f are Proton and femi energy, respectively.

Another utilized energy (dependence) for the surface (imaginary) term has been pointed out by Naik *et al.* (2021) [15] and Naik *et al.* (2020) [16] as follow:

$$A_{D,V} = W_{D,V}^{DISP} \left[1 + (-1)Z' + 1 \frac{C_{wiso,wviso}^{N-Z}}{W_{D,V}^{DISP} A} \right]. \quad (2)$$

Where, $W_{D,V}^{DISP}$ and $C_{wiso,wviso}$ are constants (undetermined), and also A , N , and Z are mass, neutron, and atomic number, respectively.

Utilized energy (dependence) for the volume (imaginary) term has been confirmed in studies of nuclear matter theory by Gopalakrishna *et al.* (2018) [17] as follow:

$$W_V(E) = A_V \frac{(E-E_f)^2}{(E-E_f)^2 + (W_V^{DISP})^2} \quad (3)$$

Where, A_V and W_V^{DISP} are constants (undetermined), and also E and E_f are proton and femi energy, respectively [18-25].

Methodology

The OPTMAN code for this work was downloaded from the IAEA website at <http://nds-IAEA.org>. The optical model code OPTMAN was chosen because it can study nucleon interactions with light-mass, medium-mass, and heavy-mass nuclei for a broad range of energy up to 200 MeV. Furthermore, it has a Soft-Rotator model in addition to its Rigid-Rotator model, which improves the precision of the even-even nuclide.

The selection of the appropriate record cards and switches determines how the code will run when the software has been successfully installed using the G-FOTRAN compiler. Record cards that describe input data are themselves described by switches for the model description. The "va" executable file is used to invoke input data of each calculation and is produced using the Windows command.

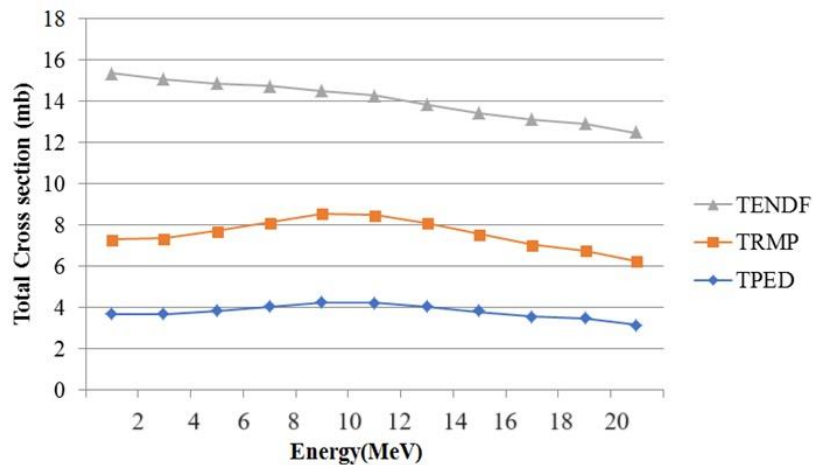
The code is executed immediately the command "va" is issued, the input file name is requested and supplied, the output file name is requested and supplied, and the enter key is pushed. The OPTMAN code computation was based on Equations (1) to (6).

Results and Analysis

The results obtained from the computer software (OPTMAN Code) based on the Equations (1) to (6) for Rotational Model Potential (RMP) which accounts for Soft-Rotator Model and Potentially Expanded by Derivatives (PED) accounts for Rigid-Rotor Model by calculating the neutron-induced Total Potentially Expanded by Derivatives (TPED), Total Rotational Model Potential (TRMP), Reaction Potentially Expanded by Derivatives (RPED), Reaction Rotational Model Potential (RRMP), Elastic Potentially Expanded by Derivatives (EPED), and Elastic Rotational Model Potential (ERMP) cross section reactions for ^{233}Pa is presented in Table 1.

Table 1: Results Obtained for Soft and Rigid-Rotor Model for Protactinium-233 (^{233}Pa)

Energy (MeV)	Cross Section (Reaction)			Cross Section (Elastic)			Cross Section (Total)		
	RPED	RRMP	RENDF	EPED	ERMP	EENDF	TPED	TRMP	TENDF
4	1.81	1.76	0.38	1.78	1.87	4.43	3.67	3.63	8.08
5	1.66	1.62	0.35	1.95	2.07	4.23	3.68	3.69	7.67
6	1.63	1.59	0.32	2.14	2.29	3.79	3.85	3.88	7.10
7	1.65	1.61	0.84	2.32	2.48	3.33	4.05	4.09	6.59
8	1.65	1.61	0.72	2.52	2.68	2.72	4.24	4.29	5.96
9	1.63	1.58	0.61	2.53	2.67	2.59	4.22	4.26	5.82
10	1.58	1.53	0.48	2.41	2.50	2.58	4.05	4.04	5.75
12	1.56	1.52	0.47	2.19	2.24	2.75	3.80	3.76	5.86
14	1.57	1.54	0.72	1.94	1.97	2.97	3.56	3.51	6.03
16	1.58	1.56	0.75	1.83	1.73	3.14	3.45	3.29	6.16
18	1.57	1.56	0.71	1.53	1.54	3.23	3.15	3.10	6.22
20	1.57	1.56	1.70	1.53	1.54	3.22	3.10	3.10	4.92

**Figure 1:** Cross Section (Total) of ^{233}Pa .

According to [Figure 1](#), the excitation function of the total cross section induced by neutrons in ^{233}Pa displays a consistent pattern: An escalation from 4 to 10 MeV followed by a decline from 10 to 20 MeV. Notably, the outcomes derived from the Total Rotational Model Potential (TRMP) exhibit a higher degree of concurrence with the data obtained from the Thermal Neutron-Induced Fission Data File

(TENDF), compared to the outcomes produced by the Total Potential Expanded by Derivatives (TPED).

In addition, the impact of rotational excitation becomes more conspicuous, with the Rotational Model Potential emerging as the optimal approach for effectively accounting for this phenomenon.

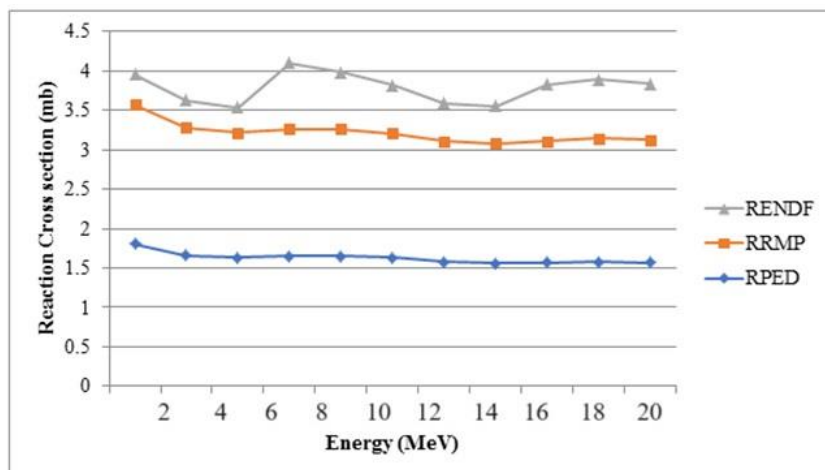


Figure 2: Reaction Cross Section of ^{233}Pa .

As depicted in Figure 2, the excitation function of Protactinium-233 exhibits a noteworthy alignment between the Potential Expanded by Derivatives (RPED) and the Rotational Model Potential (RRMP), particularly within the energy range of 4-6 MeV, as evidenced by the congruence with the established reference data (REDF). This alignment suggests that the threshold energy for neutron-induced reactions in both RPED and RRMP lies at ≤ 4 MeV. However, a marked

disparity arises between the calculated PED values and the established ENDF standard data within the energy span of 6-12 MeV. Notably, the results derived from the Rotational Model Potential exhibit superior accord with the reference data (REDF) when contrasted with the outcomes obtained from the Potential Expanded by Derivatives. This underscores the capacity of the Rotational Model Potential to effectively characterize the dynamic alterations in nuclear structure brought about by rotation.

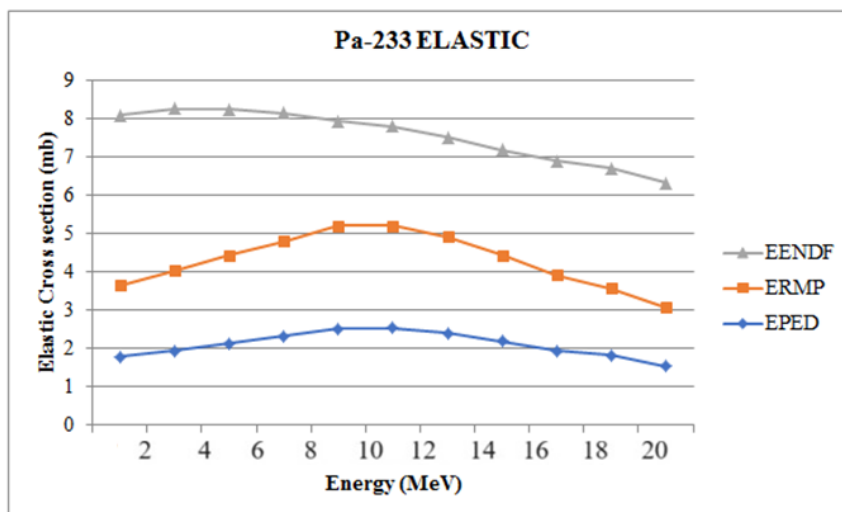


Figure 3: Elastic Cross Section of ^{233}Pa .

As demonstrated in Figure 3, a noteworthy correspondence is evident in neutron-induced elastic scattering between the Potential

Expanded by Derivatives (EPED) and the Rotational Model Potential (ERMP), specifically within the energy intervals of 4 to 6 MeV and 10

to 20 MeV, where alignment with the retrieved reference data (EENDF) is observed. However, lack of consensus emerges between EPED and the established EENDF standard data within the energy span of 6 to 9 MeV.

This discrepancy underscores the efficacy of Rotational Model Potential, which incorporates the soft-Rotor model of the Coupled-channels Optical Model, in effectively elucidating the impact of excitation-induced rotation on neutron capture. Notably, this approach exhibits a stronger concurrence with the reference data (EENDF), solidifying its suitability for describing the intricate interplay between rotation and neutron interactions.

Conclusion

A coupled-channel optical model OPTMAN code was used to investigate the effects of neutron-induced fissile isotopes of Protactinium-232. Optical model computations were carried out via the OPTMAN code using the Coupled-Channel Rotational Model Potential (CC-RMP) which described the Soft-Rotor model that treated nuclei as soft rotational sphere or deformed nuclei and Potential Expanded by Derivatives (CC-PED) which described Rigid-Rotor Model that treated nuclei as rigid vibrating sphere and account for nuclear volume conservation. From the computations performed for both PED and RMP, the energies agreed with the standard retrieved data (ENDF) are observed to be 4 MeV. It was also revealed that the results obtained from using Rotational Model Potential (RMP) are generally higher and are in better agreement with the standard ENDF data than those obtained from the Potential Expanded by Derivatives (PED).

However, results using both PED and RMP for elastic scattering cross sections are generally higher for ^{232}Pa and showed better agreement with the retrieved ENDF data. Furthermore, the odd-A nuclides tend to have higher cross section values when compared with the even-A nuclides. Since the oddness of both Z and N tends to lower the nuclear binding energy, making odd nuclei less stable and more likely to

undergo fission, all odd-A nuclei used in this research could be best for reactor fuel, except for the fissionable, but not fissile materials. It is therefore recommended that the odd-A nuclei used in this work be tested as reactor fuel.

Disclosure statement

The authors declare that they have no conflict of interest.

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